

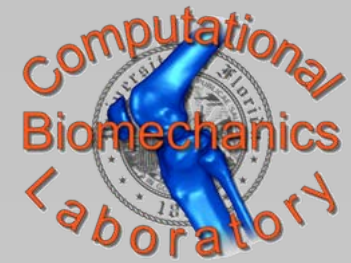
# Lecture 16

## Ground Contact Modeling

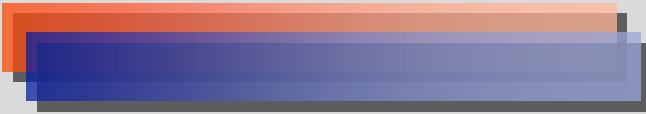
EML 5595  
Mechanics of the Human Locomotor System



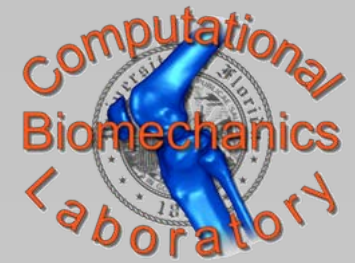
# Outline



- Motivation
- Methods
- Journal Article Review  
Neptune et al. (2000)



# Outline



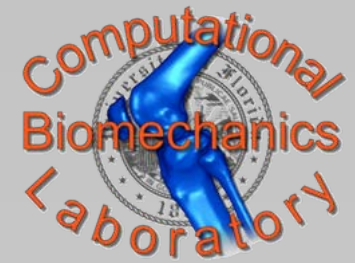
- Motivation

# Why Ground Contact Models?

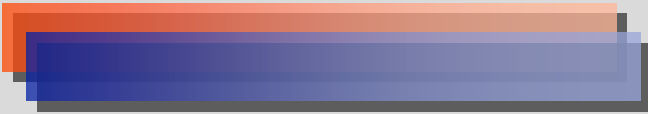
- Important human movements such as gait involve changes in ground contact conditions (e.g., single support vs. double support).
- Different movement tasks involve different ground contact conditions (e.g., compare gait and jumping).
- Constraint-based ground contact requires different models for different tasks or changing the model when ground contact conditions change.
- Deformable ground contact permits use of a single model regardless of changes in contact conditions or task (e.g., one model for gait and jumping).



# Outline



- Motivation
- **Methods**



# Modeling Methods

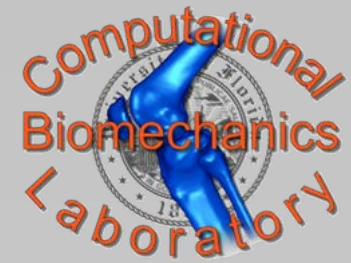
## **Constraint-based ground contact:**

- Joints (typically weld or pin) used to constrain foot to remain in contact with the ground
- Internal reaction forces and torques can be calculated in constrained directions
- Facilitates induced acceleration or power analyses
- No numerical stiffness added to system

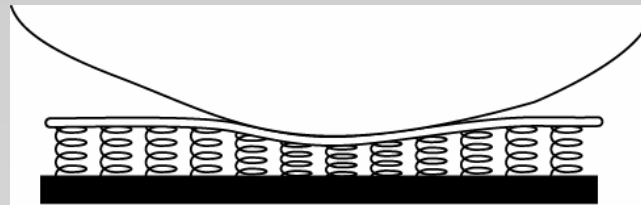
## **Deformable ground contact:**

- Discrete springs typically used to prevent foot from penetrating floor excessively
- Spring forces can be calculated at each discrete location given the current amount of interpenetration
- Complicates induced acceleration or power analyses
- Can make the system numerically stiff

# Deformable Ground Contact



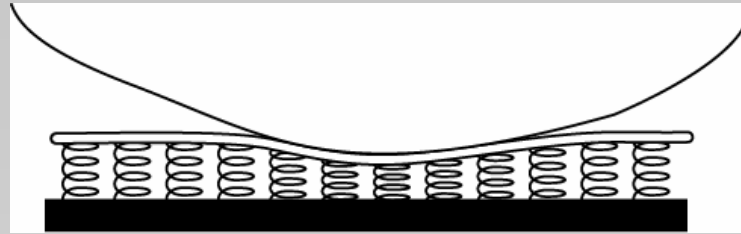
Concept: Prevent the foot from excessively penetrating the floor by placing stiff springs at discrete locations across the floor surface.



For each spring,

$$F_{norm} = kx^n$$

# Deformable Contact Issues



$$F_{norm} = kx^n$$

- 1) How do we pick  $k$ ?
- 2) Is  $k$  the same for every spring?
- 3) How do we pick  $n$ ?
- 4) How do we account for damping?
- 5) How do we account for friction?

# How to Pick $k$ and $n$ ?

- 1) Linear elastic contact model ( $n = 1$ )

$$F_i = p_i A_i$$

where

$$p_i = \frac{(1-\nu)E_i}{(1+\nu)(1-2\nu)h_i} x_i$$

so

$$k_i = \frac{(1-\nu)E_i}{(1+\nu)(1-2\nu)h_i} A_i$$

- 2) Experiments with shoes
- 3) Optimization

# How to Account for Damping?

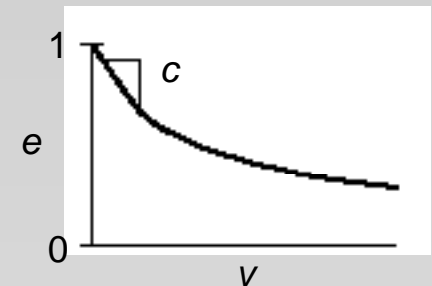
## Linear Damping

$$F = kx^n + c\dot{x}$$

Why does this commonly-used method produce unrealistic forces at contact initiation?

## Nonlinear Damping (Hunt and Crossley, 1975)

$$F = kx^n(1 + c\dot{x})$$



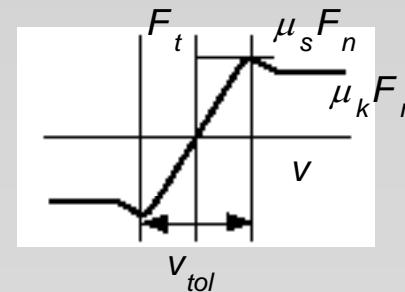
How does this damping formulation eliminate unrealistic forces at contact initiation?

# How to Account for Friction?

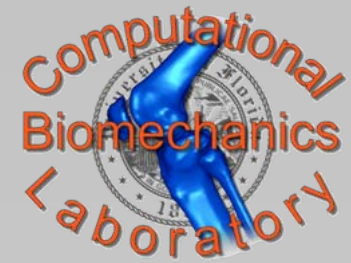
## Coulomb Friction

$$F_{\text{tan}} = \mu F_{\text{norm}}$$

applied opposite to the local sliding direction

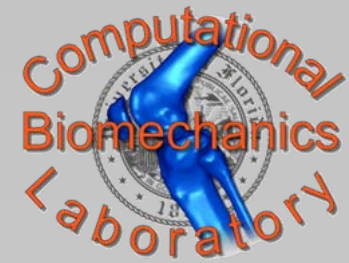


# Outline



- Motivation
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- **Journal Article Review**  
**Neptune et al. (2000)**

# Published Contact Model



- 1) What ground contact model formulation did Neptune et al. (2000) use?
- 2) What are the strengths of this formulation?
- 3) What are its weaknesses?
- 4) What ground contact model would you use, and why?