29. Use the finite element method to solve the plane truss shown below. Assume $A E=10^{6} \mathrm{~N}, L=1 \mathrm{~m}$. Determine the nodal displacements, forces in each element and the support reactions.

30. The properties of the two elements of a plane truss are given in the table below. Note that an external force of $10,000 \mathrm{~N}$ is acting on the truss at node 2 .

| Elem. | $i \rightarrow j$ | $\phi$ | $l$ | $m$ | $L(\mathrm{~m})$ | $A\left(\mathrm{~cm}^{2}\right)$ | $E(\mathrm{GPa})$ | $\alpha\left(/{ }^{\circ} \mathrm{C}\right)$ | $\Delta T\left({ }^{\circ} \mathrm{C}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $1 \rightarrow 2$ | 90 | 0 | 1 | 1 | 1 | 100 | $20 \times 10^{-6}$ | -100 |
| 2 | $2 \rightarrow 3$ | 0 | 1 | 0 | 1 | 1 | 100 | $20 \times 10^{-6}$ | 0 |

(a)

Write the thermal force vector踥
(b) Assemble the thermal force vectors to form the global thermal force $\left\{\mathbf{F}_{T}\right\}$, which is a $2 \times 1$ matrix.
(c) Solve the problem for the unknown displacements. Determine the element force $P$ in each element.
(d) Show that equilibrium is satisfied at node 2 .


